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POLYTECHNIQUE
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ON THE DESIGN OF PUBLIC TRANSPORT FOR EQUALITY OF ACCESSIBILITY

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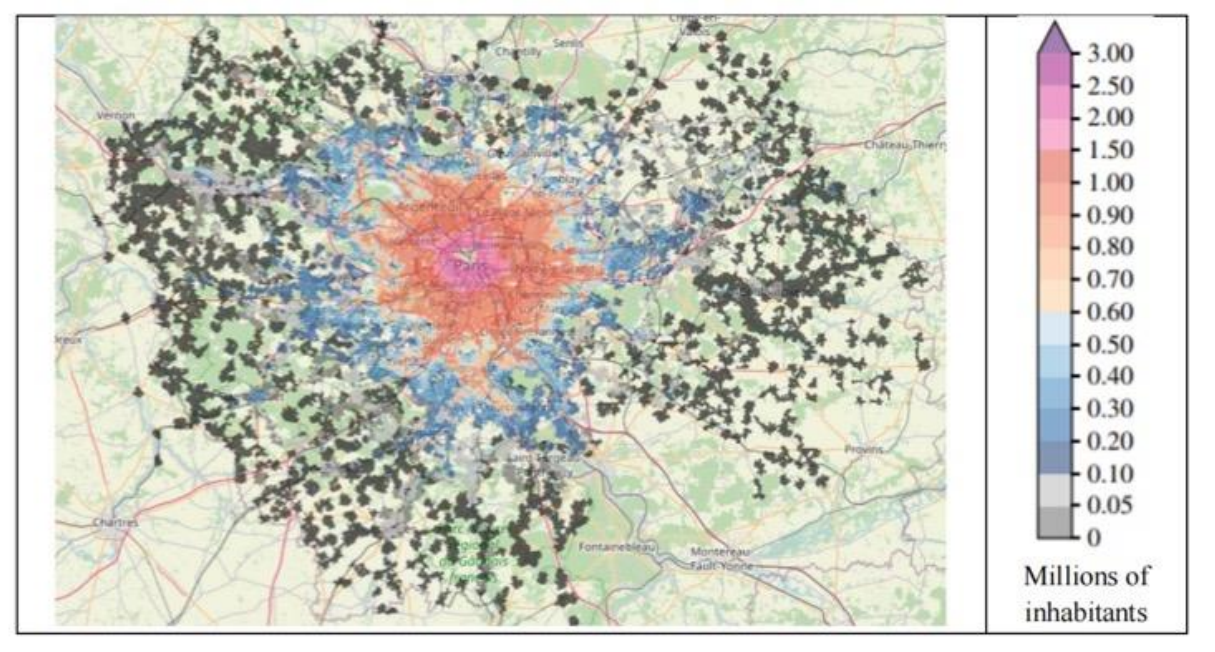
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INTRODUCTION

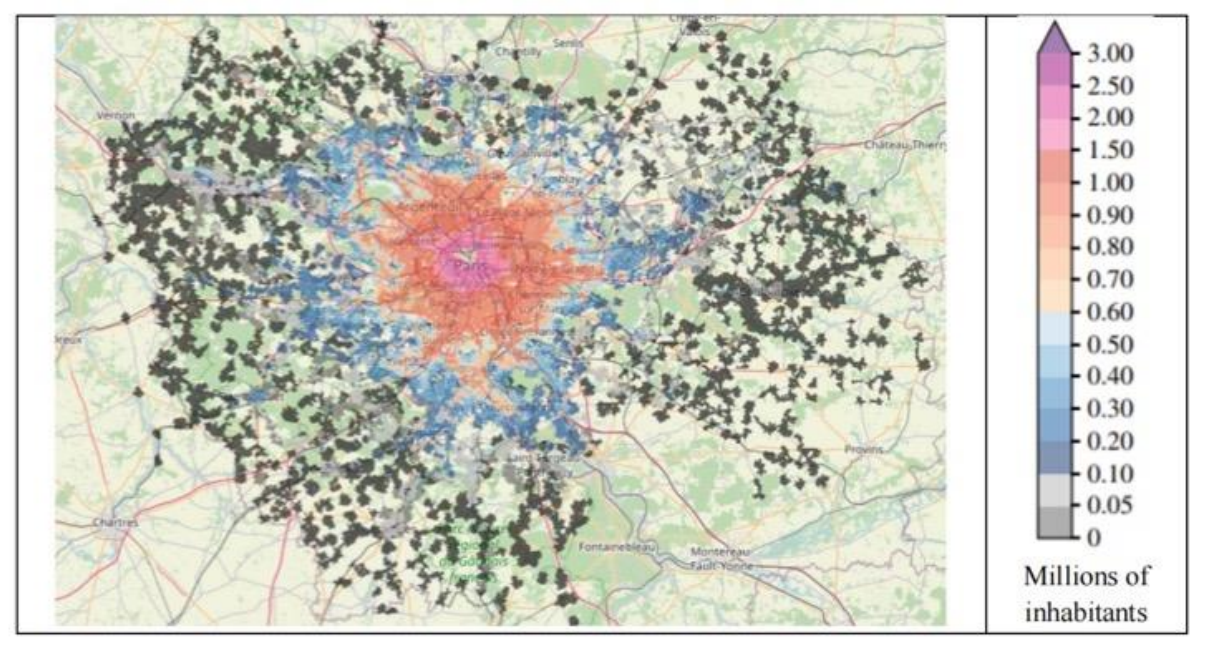


INTRODUCTION



Accessibility: ease of reaching surrounding opportunities.
Inequality: suburbs suffer from poor accessibility from public transit.

INTRODUCTION



Accessibility: ease of reaching surrounding opportunities.
Inequality: suburbs suffer from poor accessibility from public transit.

Consequence: car-dependency → pollution
Need for designing more equitable public

INTRODUCTION



OBJECTIVE

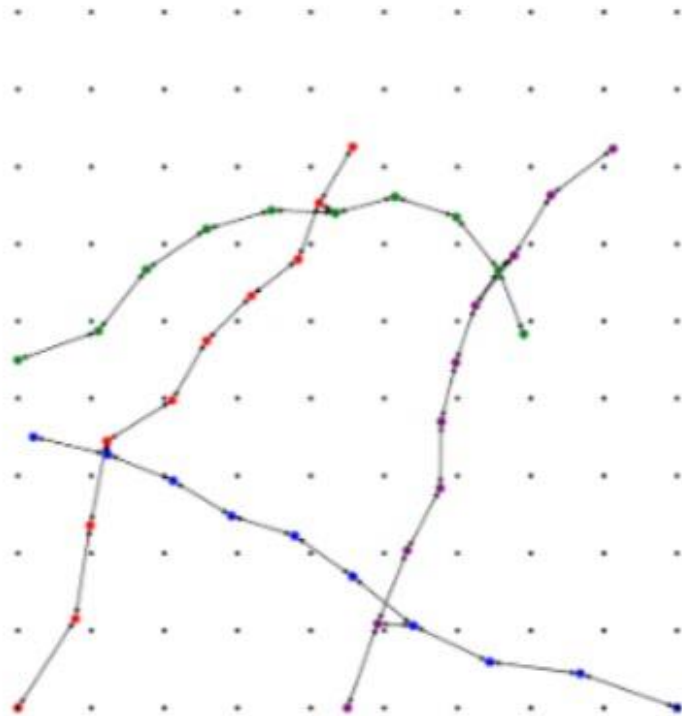
Improve equality while preserving PT efficiency
by serving or skipping PT stops



METHODOLOGY



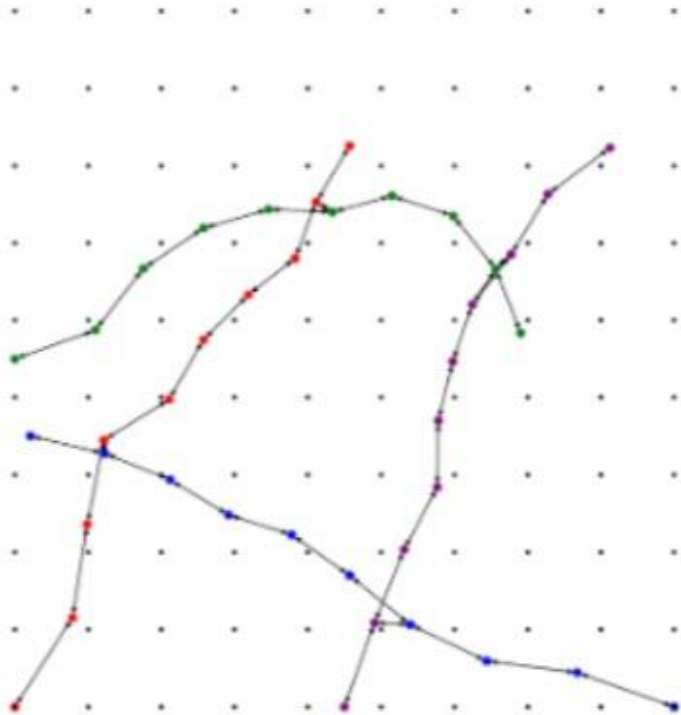
METHODOLOGY



An example of PT network: 4 PT lines containing 40 stops and 100 centroids

PUBLIC TRANSPORT (PT) AND ACCESSIBILITY

1. G : PT network
2. V : set of centroids
3. S : set of bus stops



An example of PT network: 4 PT lines containing 40 stops and 100 centroids

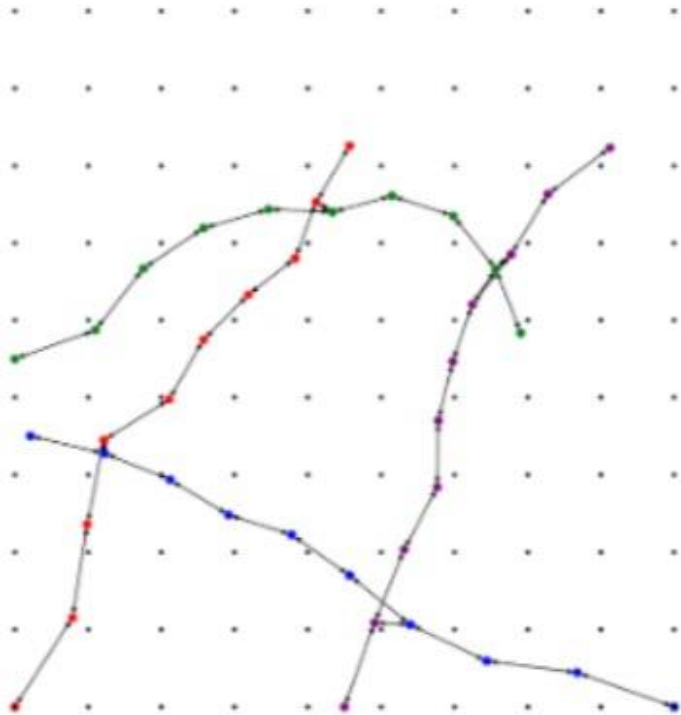
PUBLIC TRANSPORT (PT) AND ACCESSIBILITY

1. G : PT network
2. V : set of centroids
3. S : set of bus stops
4. The accessibility of centroid $v \in V$,

$$acc(v) = \sum_{u \in V} \frac{X(u)}{T(v, u)}$$

$T(v, u)$: shortest time to go from v to u ,

$X(u)$: amount of the opportunities of the u .



An example of PT network: 4 PT lines containing 40 stops and 100 centroids

PUBLIC TRANSPORT (PT) AND ACCESSIBILITY

$V^\%$: set of centroids with the worst accessibility. The accessibility of graph G as:

$$Acc(G; m) = \frac{1}{|V^\%|} \sum_{v \in V^\%} acc(v)$$

The Atkison inequality index is

$$Atk(G) = 1 - \frac{1}{\overline{acc}(G)} \cdot \left(\frac{1}{K} \sum_{i=1}^k y_i^{-1} \right)^{-1}$$



perfect equality

maximum inequality

RANDOM SEARCH OPTIMIZATION ALGORITHM

1. Ef-Opt: maximize the average accessibility
2. Eq-Opt: maximize the accessibility of the worst centroids

Algorithm 1: Random search optimization algorithm

- 1: **Input** Public transport graph \mathcal{G} with stops \mathcal{S} .
Parameter m of the accessibility formula (2).
 - 2: **For** search instance $i \leftarrow 1$ to n :
 - 3: Initialize $\mathcal{G}_0 \leftarrow \mathcal{G}$ and $\mathcal{S}_0 \leftarrow \mathcal{S}$.
 - 4: **For** step $t \leftarrow 0$ to ∞ until **termination condition**:
 - 5: Select a random stop $s_t \in \mathcal{S}_t$ and deactivate it.
 - 6: Set $\mathcal{S}_{t+1} \leftarrow \mathcal{S}_t \setminus \{s_t\}$ and let \mathcal{G}_{t+1} the resulting PT graph.
 - 7: Compute the new accessibility: $Acc(\mathcal{G}_{t+1}; m)$
 - 8: **EndFor**
 - 9: Record $\mathcal{G}^i = \arg \min_{\tau=0}^{t+1} Acc(\mathcal{G}_\tau, m)$.
 - 10: **EndFor**
 - 11: **Return** PT graph $\mathcal{G}^* = \arg \min_{i=1}^n \mathcal{G}^i$.
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RESULTS



RESULTS

Performance on the entire data set

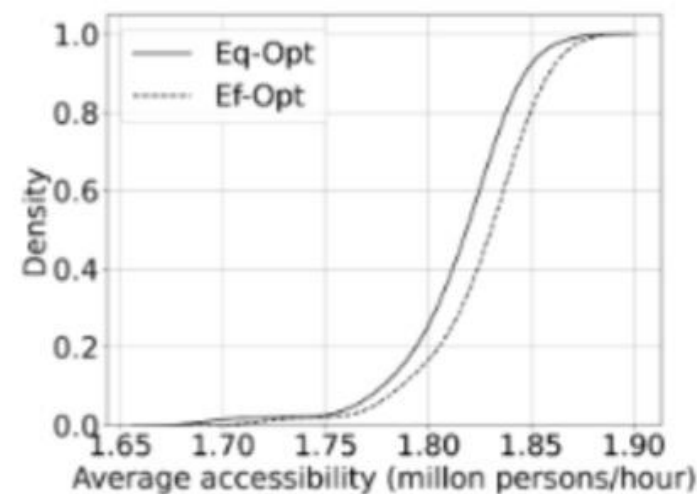
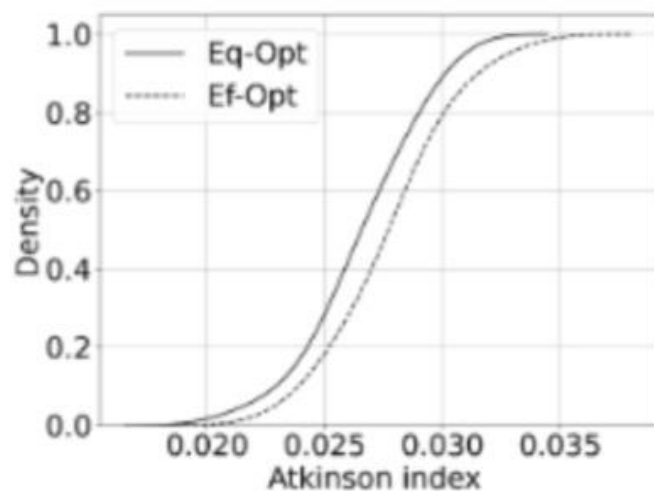


Figure 2: Cumulative Distribution Functions (CDFs) of Atkinson index and average accessibility after Eq-Opt and Ef-Opt

RESULTS

Performance on each graph

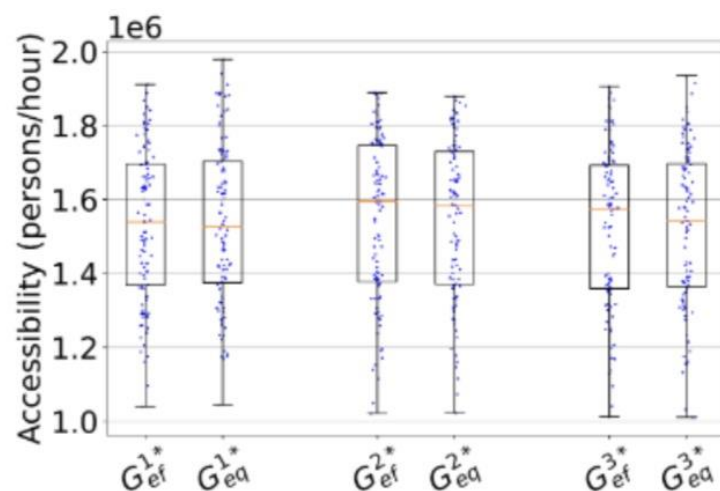


Figure 3: Change in the distribution of accessibility across centroids in three exemplary graphs.

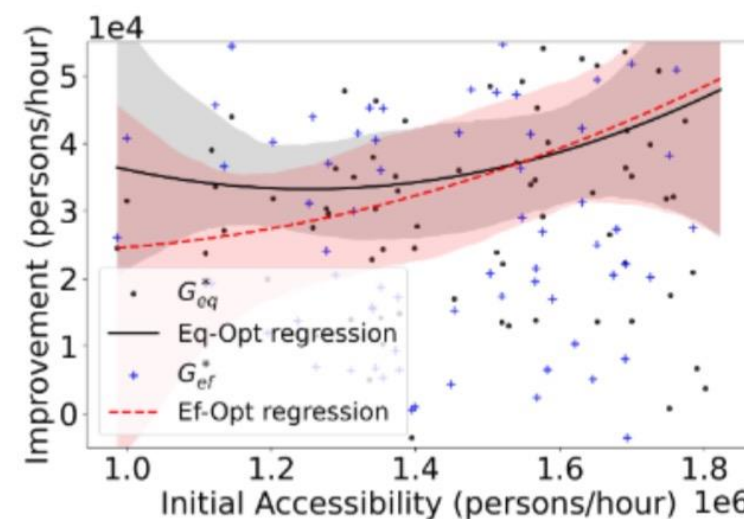


Figure 4: Change in accessibility on one exemplary graph.

RESULTS

The difference between selection strategies

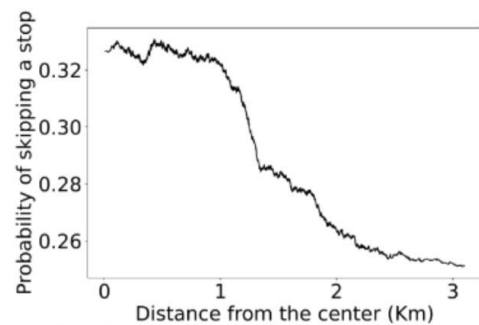


Figure 5: Relation between the probability of skipping a stop and distance from the center by Eq-Opt

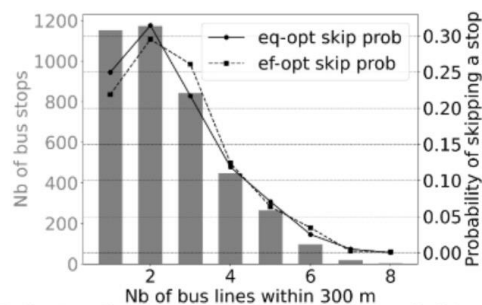


Figure 6: Relation between the probability of skipping a stop and the Nb of bus lines nearby

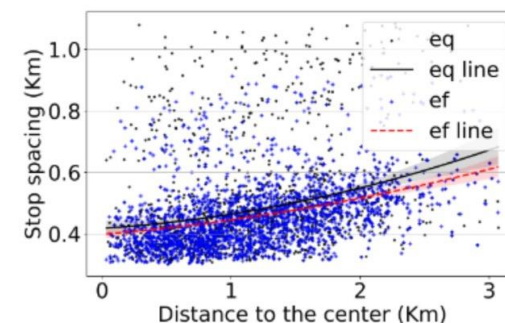


Figure 7: Relation between the distance to the nearest stop and the distance to the center



FUTURE WORK



FUTURE WORK

1. Apply optimization to real PT network data (GTFS)
2. Consider the deployment of shared mobility
3. Use Deep-Q learning to select stops