



# Formal Approaches for Testing against Non-deterministic Specifications & Related Complexity Issues

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**04, December, 2018**



# Motivation

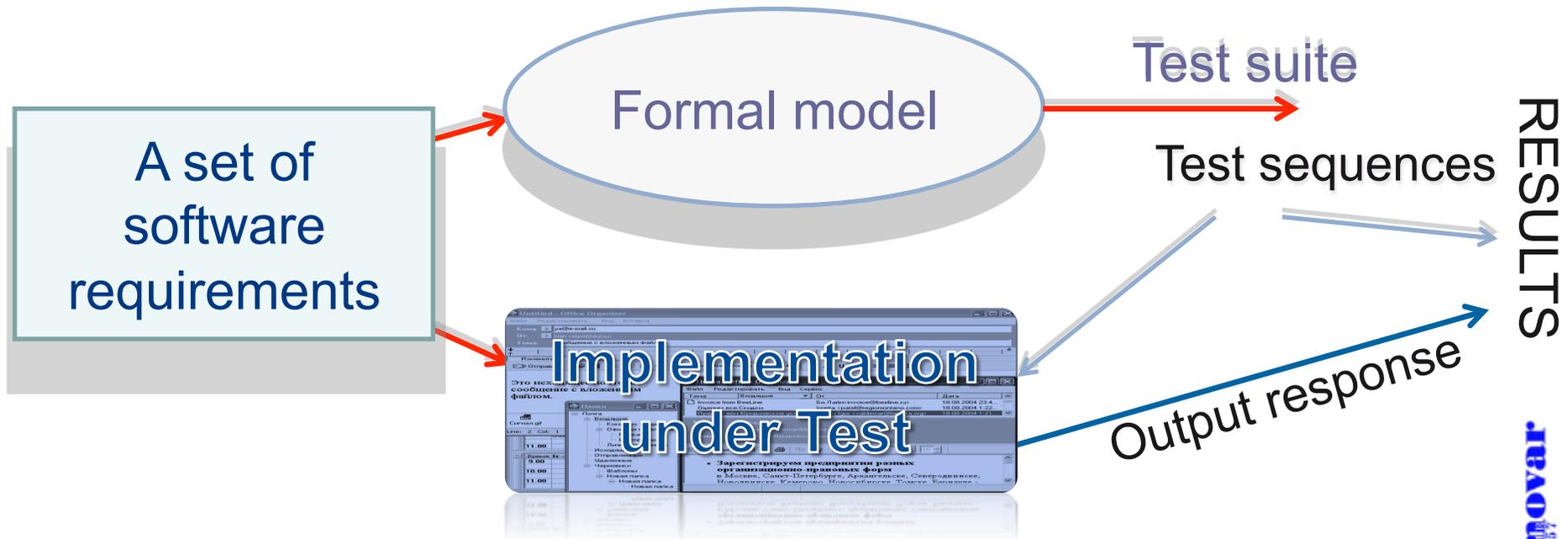
- Every information system has software and hardware components (often from different providers)
- The quality of the corresponding components needs to be verified thoroughly
- Tests with guaranteed fault coverage can be derived only when addressing to formal models
- Guaranteed fault coverage requires lots of assumptions
- Testing should be scalable enough



**Novel testing approaches should be developed**  
**Complexity should be estimated / decreased**



# Model based testing



## Testing steps:

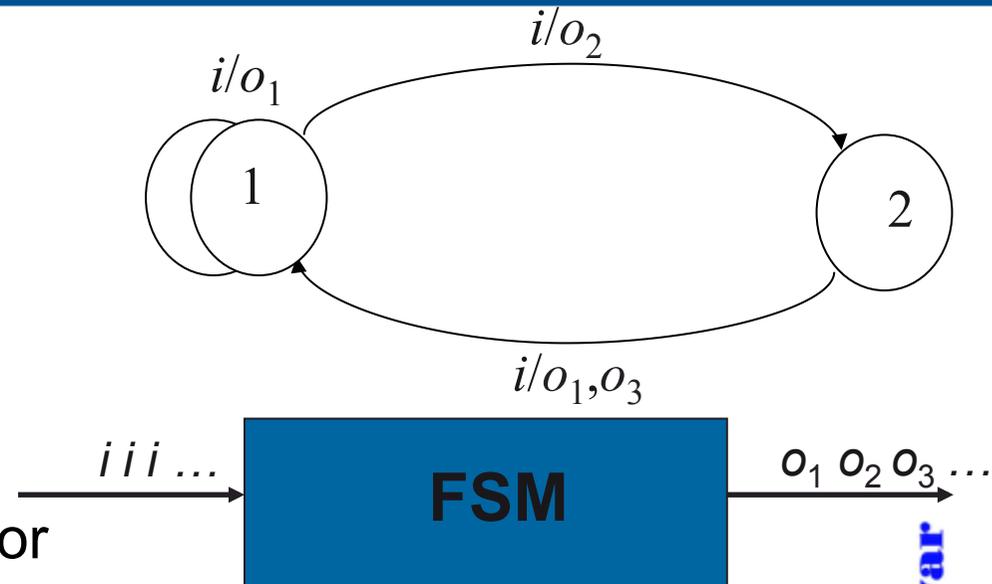
- ↓ deriving test sequences
- ↓ applying the test sequences against a given IUT
- ↓ drawing a conclusion about the correctness of the IUT

**For reactive systems, Finite State Machines are widely used as Formal Models**

# Finite State Machine (FSM)

$\zeta = \langle S, I, O, h_S, S' \rangle$  is an FSM

- $S$  is a finite set of states  
 $S'$  is a subset of initial states
- $I$  and  $O$  are finite input and output alphabets
- $h_S \subseteq S \times I \times O \times S$  is a behavior relation



Can be

- *Complete or partial*
- *Deterministic or not*
- *Observable or not*
- ...

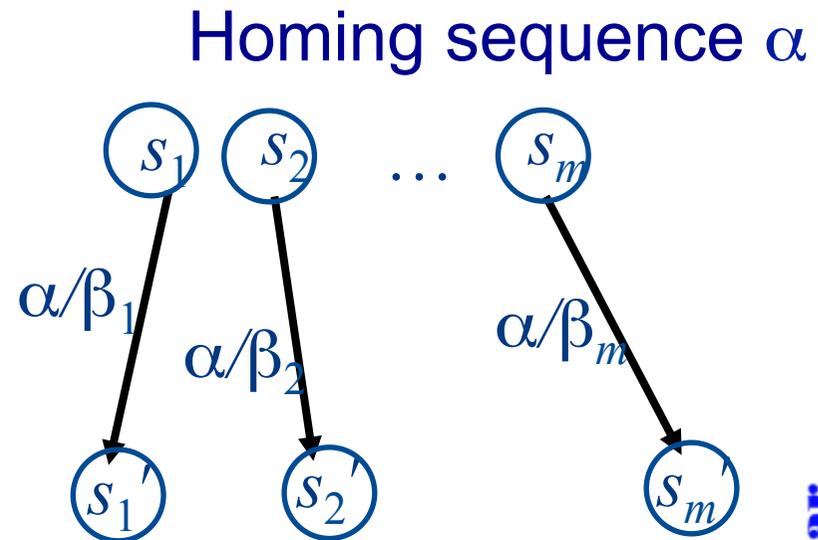
Telecommunication protocols can be highly non-deterministic, due to the optionality

**Test suite derivation is based on the effective initial / final state identification**



# Homing sequence (HS)

- $\alpha$  allows to detect the final state of the machine after  $\alpha$  is applied
- After applying  $\alpha$  at state  $s_i$  and observing an output response  $\beta_i$  the final state  $s_i'$  becomes known



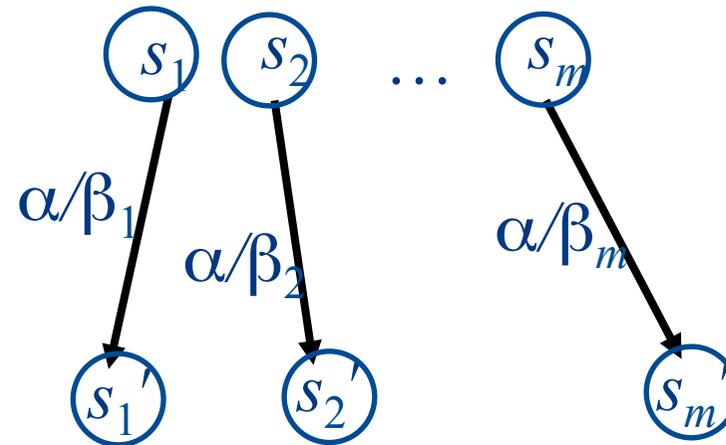
Applying  $\alpha$  + observing  $\beta_i \rightarrow$  drawing a conclusion about  $s_i'$

- **We proposed methods for final state identification for partial and/or non-deterministic specifications [1]**
- **We also estimated the related complexity [2]**

# Distinguishing sequence (DS)

- $\alpha$  allows to detect the initial state of the machine
- After applying  $\alpha$  at state  $s_i$  and observing an output response  $\beta_i$ , the initial state  $s_i$  becomes known

Distinguishing sequence  $\alpha$



$$out(s_i, \alpha) \cap out(s_j, \alpha) = \emptyset$$

- **We proposed methods for initial state identification for partial and non-observable specifications**
- **We also estimated the related complexity [3]**

# Bad... very bad 'news'

*Most of the problems in the area of model based testing are NP/PSPACE-complete*

- **Checking the existence of a distinguishing sequence for complete deterministic FSMs is PSPACE-complete**
- **Learning a deterministic FSM under a given set of input/output sequences is NP-complete**
- **Checking the existence of a homing sequence for partial deterministic FSMs is PSPACE-complete [2]**
- **The length of a distinguishing sequence for a complete non-deterministic FSM with  $n$  states is in the worst case  $O(2^n)$  [3]**
- ...



# How to decrease the complexity?

Utilizing **scalable representations** allows to 'hide' the complexity

- **Logic circuits**
- **Test Cases as FSMs**

Providing **effective heuristics**  
**Specific truncating rules for the successor tree + effective traversal**

Considering **specific types of bugs in the software**, i.e., specific fault models

- **White Box Testing**
- **User Defined Faults**

Switching from **preset to adaptive** test derivation strategy

- **DS for non-deterministic FSMs**
- **HS for non-deterministic FSMs**

*All of them are good for well-defined types of specifications*

# One of the test generation approaches with the reduced complexity

**We propose how to derive tests with the guaranteed fault coverage w.r.t. the fault model  $\langle \zeta, \approx, FD \rangle$  [4]**

$\zeta$  can be **partial and non-deterministic** (non-observable even) but initialized



- How to distinguish between  $\zeta$  and a mutant  $M \in FD$ ?

$FD$  is explicitly enumerated  $\rightarrow$  complexity reduction trick

- A DS for the direct sum  $\zeta \oplus M$  can be derived
- $\zeta \oplus M$  contains all the transitions that are included into FSM  $\zeta$  and FSM  $M$

# DS derivation for a partial non-deterministic FSM

$$S' = \{s_1, s_2\}$$

- Derive a truncated successor tree (TST)

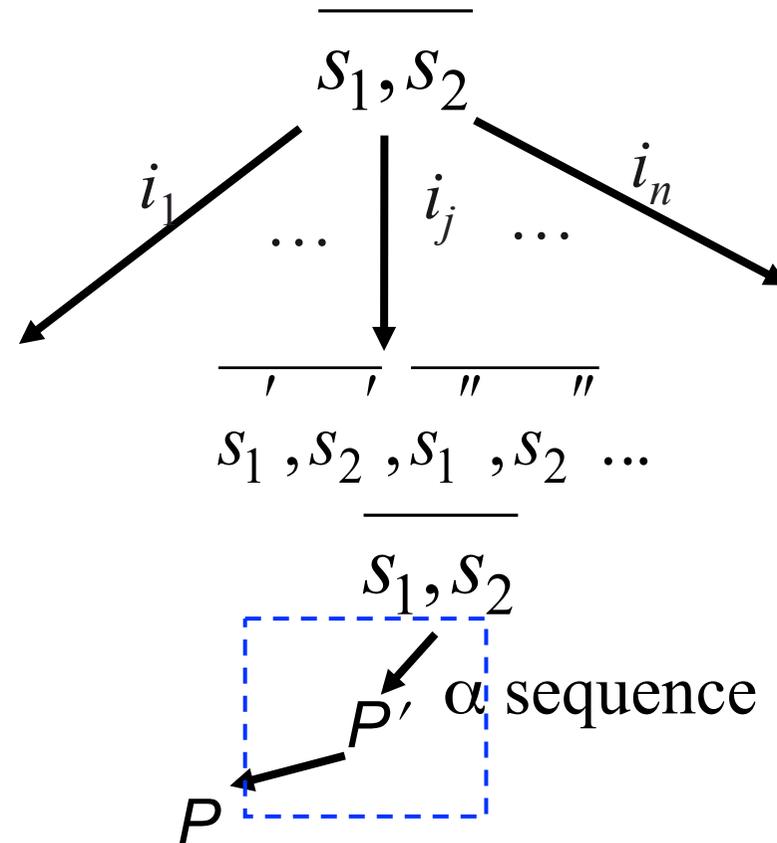
$$\exists o_1 ((s_1, i_j, o_1, s_1', ) \in h_S \ \& \ (s_2, i_j, o_1, s_2') \in h_S \ \& \ s_1' \neq s_2')$$

- Truncating rules

**Rule 1**  $P$  is the empty set

**Rule 2** Set  $P$  contains a subset that labels another node of the path from the root to the node labeled by the set  $P$

**Rule 3**  $P$  contains singleton



**$\alpha$  is a distinguishing sequence iff it labels the path truncated by Rule 1**

# Deriving a test suite $TS$ w.r.t. $\langle \zeta, \approx, FD \rangle$

**Input:** FSM  $\zeta$  which is initialized

**Output:** A test  $TS$  for  $\zeta$  or a corresponding message

**Step 1**  $i = 0$

**Step 2**

Derive a current mutant  $M_i$  for the FSM  $\zeta$

**Derive a distinguishing sequence**  $\alpha$  for the pair of initial states of FSM  $M_i \oplus \zeta$

If there is no distinguishing sequence for the pair of initial states of the FSM  $M_i \oplus \zeta$ , then

**Return** a corresponding message

Otherwise,

If  $\alpha \notin TS$  then add  $\alpha$  into the test suite  $TS$

$i++$ , and go to **Step 2**

# The test suite length can be polynomial

Partial non-observable  
specification  $\xi$

Deterministic/  
observable FSM  $\xi^o$

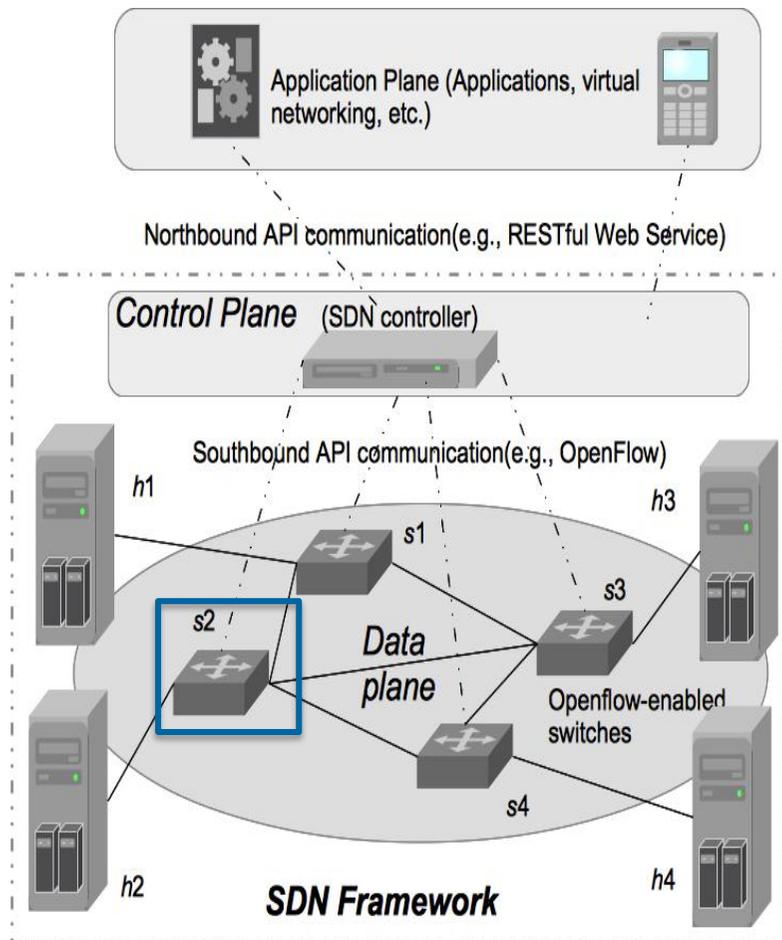
**Maybe, the specification is  
'good', i.e., allows an observable  
projection [5]?**

Adaptive sequence (of a polynomial length) can be  
derived for the FSM  $M_i^o \oplus \xi^o$

The number of mutants  $|FD|$  can also be polynomial

**There can be an exhaustive test suite of a polynomial length  
w.r.t.  $\langle \xi, \approx, FD \rangle$  [4]**

# One of the possible applications



- An SDN-enabled switch is an SUT
- How to assure the reliable packet delivery???



- We consider a Fault Model  $\langle \zeta, =, FD \rangle$
- The specification  $\zeta$  is modeled via a logic circuit [6]
- User-Defined faults identify the mutants
- Distinguishing patterns for each mutant form the test suite

**Our test suite detects the output and parameter faults in the action / matching part of the rules**

# Conclusions

- **Theoretically:** almost all the problems in (software) testing with guaranteed fault coverage have terrible complexity
- **Practically:** methods and tools for decreasing the complexity seem to be promising



**New models need to appear and new methods and tools need to be provided to decrease the complexity**



We do have something to tackle as a future work 😊



## (Selected) references

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2. Hüsnü Yenigün, Nina Yevtushenko, Natalia Kushik: The complexity of checking the existence and derivation of adaptive synchronizing experiments for deterministic FSMs. Inf. Process. Lett. 127: 49-53 (2017)
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4. Hüsnü Yenigün, Natalia Kushik, Jorge López, Nina Yevtushenko, Ana R. Cavalli: Decreasing the complexity of deriving test suites against nondeterministic finite state machines. EWDTS 2017: 1-4
5. Natalia Kushik, Hüsnü Yenigün: Heuristics for Deriving Adaptive Homing and Distinguishing Sequences for Nondeterministic Finite State Machines. ICTSS 2015: 243-248
6. Asma Berriri, Jorge López, Natalia Kushik, Nina Yevtushenko, Djamel Zeglache: Towards Model based Testing for Software Defined Networks. ENASE 2018: 440-446
7. ...





# THANK YOU!



METHODES